

**CBSE - X**

# SIMILAR TRIANGLES

REVISION MODULE

Embark on a concise yet comprehensive revision of Similar Triangles with our specialized study module designed for CBSE Class 10 Mathematics. This resource is meticulously crafted to provide a quick and effective review of key concepts, ensuring proficiency in this essential aspect of geometry.



*The Success Destination*

Prepare for success in CBSE Class 10 Mathematics with confidence in Similar Triangles. Order our revision module now to embark on a quick and effective review journey, reinforcing your knowledge in this vital aspect of geometry!



# SIMILAR TRIANGLES

## REVISION MODULE CBSE-MATHEMATICS

### Fundamental Concepts:

- Revisit the fundamental concepts of Similar Triangles, understanding the criteria that determine their similarity.

### Similarity Criteria:

- Explore the different criteria for establishing similarity between triangles, including the Angle-Angle (AA) criterion, Side-Angle-Side (SAS) criterion, and Side-Side-Side (SSS) criterion.

### Basic Proportionalities:

- Understand the basic proportionalities that exist between corresponding sides and angles of similar triangles. Reinforce your knowledge of the proportional relationship between corresponding altitudes and medians.

### Theorems and Consequences:

- Review important theorems related to similar triangles, such as the Basic Proportionality Theorem (Thales Theorem) and the Converse of Basic Proportionality Theorem.

### Problem-Solving Practice:

- Hone your problem-solving skills with targeted revision questions. The module includes questions of varying difficulty levels, ensuring a comprehensive preparation for the CBSE Class 10 Mathematics examination.

### Application of Similar Triangles:

- Connect theoretical knowledge to practical applications. Explore the diverse applications of similar triangles in real-world scenarios, from surveying to indirect measurement.

### Visual Learning Aids:

- Enhance your comprehension with visual aids, diagrams, and illustrations. Visual representations make abstract concepts related to similar triangles visually tangible, aiding in better understanding and retention.

### Time-Efficient Revision:

- Optimize your revision time with a focused and condensed review of Similar Triangles. The module is designed for efficient revision, allowing you to reinforce your knowledge in a short span.

### Accessible Anytime, Anywhere:

- Access the revision module online at your convenience. The digital platform offers flexibility for efficient and personalized revision, allowing you to tailor your study schedule for optimal results.



# SIMILAR TRIANGLES

REVISION  
 MODULE: 04

## Basic Concepts

- **Similar Figures:** Two figures are said to be similar, if they have same shape but not necessarily the same size.
- **Conditions of Similarity of Figures:** The condition of similarity of different figures are as follows:
  - (i) **Line segment:** Two lines segments are always similar.
  - (ii) **Circle:** Two circles are always similar.
  - (iii) **Square:** Two squares are always similar.
  - (iv) **Equilateral triangle:** Two equilateral triangles are always similar.
  - (v) **Polygon:** Two polygons of the same number of sides are similar if
    - (a) their corresponding angles are equal.
    - (b) the length of their corresponding sides are proportional.
  - (vi) **Triangle:** Two triangles are said to be similar iff
    - (a) their corresponding angles are equal and
    - (b) their corresponding sides are in the same ratio (or proportional).

i.e.,  $\triangle ABC$  and  $\triangle DEF$  are said to be similar iff  $\angle A = \angle D$ ,  $\angle B = \angle E$ ,  $\angle C = \angle F$  and

$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}. \text{ It is written as } \triangle ABC \sim \triangle DEF.$$

### Some Basic Theorems on Similarity of Triangles:

- **Theorem 1 (Basic Proportionality Theorem or Thales Theorem):**

**Statement:** If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio.

**Given:** A triangle  $ABC$  in which a line parallel to side  $BC$  intersects other two sides  $AB$  and  $AC$  at  $D$  and  $E$  respectively.

**To Prove:**  $\frac{AD}{DB} = \frac{AE}{EC}$

**Construction:** Join  $BE$  and  $CD$  and then draw  $DM \perp AC$  and  $EN \perp AB$ .

**Proof:** Area of  $\triangle ADE = \frac{1}{2} \text{ base} \times \text{height}$

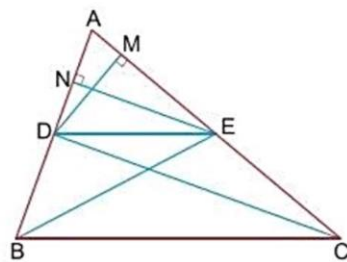


Fig. 7.1

So,  $ar(\triangle ADE) = AD \times EN$

and  $ar(\triangle BDE) = DB \times EN$

Similarly,  $ar(\triangle ADE) = \frac{1}{2} AE \times DM$

and  $ar(\triangle DEC) = \frac{1}{2} EC \times DM$

Therefore,  $\frac{ar(\triangle ADE)}{ar(\triangle BDE)} = \frac{\frac{1}{2} AD \times EN}{\frac{1}{2} DB \times EN} = \frac{AD}{DB}$  ... (i)

and  $\frac{ar(\triangle ADE)}{ar(\triangle DEC)} = \frac{\frac{1}{2} AE \times DM}{\frac{1}{2} EC \times DM} = \frac{AE}{EC}$  ... (ii)

Now,  $\triangle BDE$  and  $\triangle DEC$  are on the same base  $DE$  and between the same parallel lines  $BC$  and  $DE$ .

So,  $ar(\triangle BDE) = ar(\triangle DEC)$  ... (iii)

Therefore, from (i), (ii) and (iii) we have,  $\frac{AD}{DB} = \frac{AE}{EC}$ .

□ **Criteria for Similarity of Triangles:**

- (i) If in two triangles, corresponding angles are equal, then their corresponding sides are in the same ratio (or proportional) and hence the two triangles are similar.

*i.e.*,  $\angle A = \angle D, \angle B = \angle E, \angle C = \angle F$

$\Rightarrow \frac{AB}{DE} = \frac{AC}{DF} = \frac{BC}{EF}$

It is known as **AAA** similarity criterion.

- (ii) If in two triangles, sides of one triangle are proportional to (*i.e.*, in the same ratio of) the sides of the other triangle, then their corresponding angles are equal and hence the two triangles are similar.

*i.e.*,  $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$

$\Rightarrow \angle A = \angle P, \angle B = \angle Q, \angle C = \angle R$

It is known as **SSS** similarity criterion.

- (iii) If one angle of a triangle is equal to one angle of the other triangle and the sides including these angles are in proportion, then the two triangles are similar.

*i.e.*  $\angle A = \angle P$  and  $\frac{AB}{PQ} = \frac{AC}{PR}$

$\Rightarrow \triangle ABC \sim \triangle PQR$

It is known as **SAS** similarity criterion.

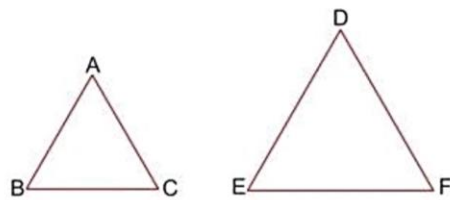


Fig. 7.2

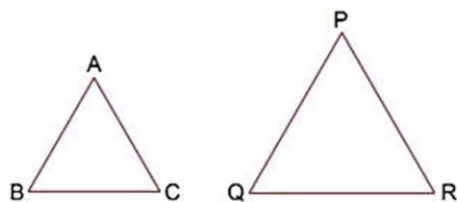


Fig. 7.3

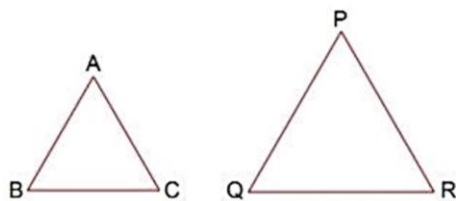


Fig. 7.4

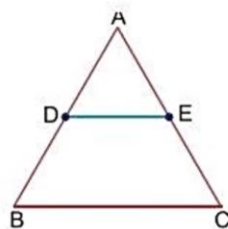


Fig. 7.5

**Important Facts/Tips:**

- (i) All congruent figures are similar but converse is not true.  
 (ii) If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side. (It is also called converse of basic proportionality theorem).

For example: In  $\triangle ABC$ ,  

$$\frac{AD}{DB} = \frac{AE}{EC} \Rightarrow DE \parallel BC.$$

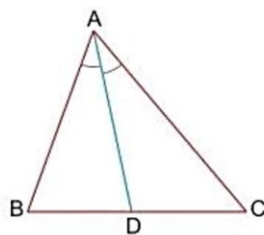


Fig. 7.6

- (iii) The internal bisector of an angle of a triangle divides the opposite side internally in the ratio of the sides containing the angle.

For example: If  $AD$  is bisector of  $\angle BAC$  in  $\triangle ABC$ , then

$$\frac{BD}{CD} = \frac{AB}{AC}$$

(iv)  $\triangle ABC \sim \triangle DEF \Rightarrow \angle A = \angle D, \angle B = \angle E, \angle C = \angle F$

$$\triangle ABC \sim \triangle FED \Rightarrow \angle A = \angle F, \angle B = \angle E, \angle C = \angle D$$

and  $\triangle ABC \sim \triangle EFD \Rightarrow \angle A = \angle E, \angle B = \angle F, \angle C = \angle D$

- (v) If  $\triangle ABC \sim \triangle DEF$ , then  $AB$  is said to be corresponding side of  $DE$  and vice-versa because opposite angle of  $AB$  i.e.  $\angle C =$  opposite angle of  $DE$  i.e.  $\angle F$ . Similarly it is applicable for other sides also.

- (vi) **Corollary of Basic Proportionality Theorem (Thales Theorem):**

In  $\triangle ABC$ , if  $DE \parallel BC$  then

$$\frac{AD}{AB} = \frac{AE}{AC}$$

**Proof:** By Thales theorem

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{DB}{AD} = \frac{EC}{AE} \quad (\text{Reciprocal})$$

Adding both sides 1, we have

$$\frac{DB}{AD} + 1 = \frac{EC}{AE} + 1$$

$$\frac{DB + AD}{AD} = \frac{EC + AE}{AE}$$

$$\Rightarrow \frac{AB}{AD} = \frac{AC}{AE}$$

$$\Rightarrow \frac{AD}{AB} = \frac{AE}{AC} \quad (\text{Again reciprocal})$$

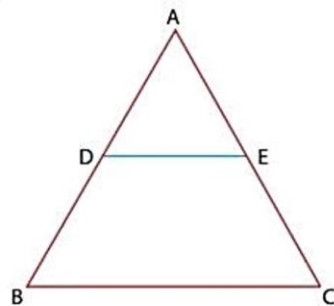


Fig. 7.7

- (vii) **AA similarity (Corollary of AAA similarity):** If two angles of one triangle are respectively equal to two angles of another triangle, then the two triangles are similar.

**Proof:** Let  $\triangle ABC$  and  $\triangle DEF$  be two triangles in which

$$\left. \begin{array}{l} \angle A = \angle D \\ \angle B = \angle E \end{array} \right\} \dots(i)$$

$$\therefore \angle A + \angle B + \angle C = \angle D + \angle E + \angle F = 180^\circ$$

$$\Rightarrow \angle A + \angle B + \angle C = \angle A + \angle B + \angle F \quad [\text{From (i)}]$$

$$\Rightarrow \angle C = \angle F$$

$$\text{i.e., } \angle A = \angle D, \angle B = \angle E \text{ and } \angle C = \angle F \Rightarrow \triangle ABC \sim \triangle DEF$$

### Selected NCERT Questions

1. In the given Fig. 7.8, if  $ABCD$  is a trapezium in which  $AB \parallel CD$ ,  $E$  and  $F$  are points on non-parallel sides  $AD$  and  $BC$  respectively such that  $EF$  is parallel to  $AB$ , then prove that

$$\frac{AE}{ED} = \frac{BF}{FC}$$

[CBSE 2020(30/1/1)]

**Sol.** We have  $ABCD$  as a trapezium.

Join  $AC$  which intersect  $EF$  at  $G$  (Fig. 7.9).

Now, in  $\triangle CAB$ , we have

$$GF \parallel AB$$

$$\Rightarrow \frac{AG}{CG} = \frac{BF}{FC} \quad (\text{BPT}) \quad \dots(i)$$

Also, in  $\triangle ADC$ , we have  $EG \parallel DC$

$$\Rightarrow \frac{AE}{ED} = \frac{AG}{GC} \quad (\text{BPT}) \quad \dots(ii)$$

From equations (i) and (ii), we get

$$\frac{AE}{ED} = \frac{BF}{FC}$$



Fig. 7.8

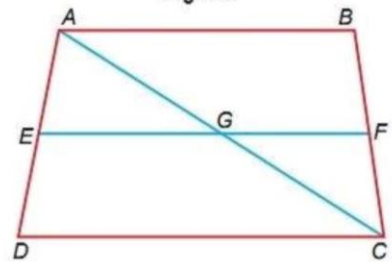


Fig. 7.9

2.  $E$  and  $F$  are points on the sides  $PQ$  and  $PR$  respectively of a  $\triangle PQR$ . Show that  $EF \parallel QR$  if  $PQ = 1.28$  cm,  $PR = 2.56$  cm,  $PE = 0.18$  cm and  $PF = 0.36$  cm.

**Sol.** We have,  $PQ = 1.28$  cm,  $PR = 2.56$  cm

$$PE = 0.18 \text{ cm}, PF = 0.36 \text{ cm}$$

$$\text{Now, } EQ = PQ - PE = 1.28 - 0.18 = 1.10 \text{ cm}$$

$$\text{and } FR = PR - PF = 2.56 - 0.36 = 2.20 \text{ cm}$$

$$\text{Now, } \frac{PE}{EQ} = \frac{0.18}{1.10} = \frac{18}{110} = \frac{9}{55}$$

$$\text{and, } \frac{PF}{FR} = \frac{0.36}{2.20} = \frac{36}{220} = \frac{9}{55} \quad \therefore \frac{PE}{EQ} = \frac{PF}{FR}$$

Therefore,  $EF \parallel QR$  [By the converse of Basic Proportionality Theorem]

3. In Fig. 7.11, if  $LM \parallel CB$  and  $LN \parallel CD$ , prove that  $\frac{AM}{AB} = \frac{AN}{AD}$ .

**Sol.** Firstly, in  $\triangle ABC$ , we have

$$LM \parallel CB \quad (\text{Given})$$

Therefore, by Basic Proportionality Theorem, we have

$$\frac{AM}{AB} = \frac{AL}{AC} \quad \dots(i)$$

Again, in  $\triangle ACD$ , we have

$$LN \parallel CD \quad (\text{Given})$$

$\therefore$  By Basic Proportionality Theorem, we have

$$\frac{AN}{AD} = \frac{AL}{AC} \quad \dots(ii)$$

Now, from (i) and (ii), we have  $\frac{AM}{AB} = \frac{AN}{AD}$ .

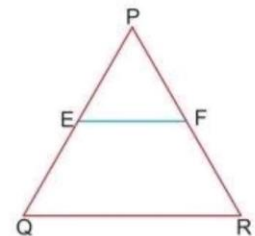


Fig. 7.10

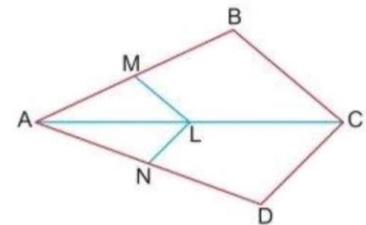


Fig. 7.11

4. In Fig. 7.12,  $DE \parallel OQ$  and  $DF \parallel OR$ , Show that  $EF \parallel QR$ .

Sol. In  $\triangle POQ$ , we have

$$DE \parallel OQ \text{ (Given)}$$

$\therefore$  By Basic Proportionality Theorem, we have

$$\frac{PE}{EQ} = \frac{PD}{DO} \quad \dots(i)$$

Similarly, in  $\triangle POR$ , we have

$$DF \parallel OR \text{ (Given)}$$

$$\frac{PD}{DO} = \frac{PF}{FR} \quad \dots(ii)$$

Now, from (i) and (ii), we have

$$\frac{PE}{EQ} = \frac{PF}{FR} \quad \Rightarrow \quad EF \parallel QR$$

[Applying the converse of Basic Proportionality Theorem in  $\triangle PQR$ ]

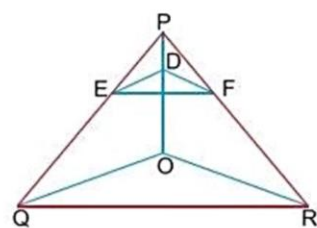


Fig. 7.12

5. The diagonals of a quadrilateral  $ABCD$  intersect each other at the point  $O$  such that  $\frac{AO}{BO} = \frac{CO}{DO}$ . Show that  $ABCD$  is a trapezium.

Sol.  $\frac{AO}{BO} = \frac{CO}{DO}$  (Given)

$$\Rightarrow \frac{AO}{CO} = \frac{BO}{DO} \quad \dots(i)$$

In  $\triangle ABD$ ,  $EO \parallel AB$  (Construction)

$$\therefore \frac{AE}{ED} = \frac{BO}{DO} \quad \dots(ii)$$

From equations (i) and (ii)

$$\frac{AE}{ED} = \frac{AO}{CO} \quad \Rightarrow \quad EO \parallel DC \quad \text{(Converse of BPT)}$$

But  $EO \parallel AB$  (Construction)

$$\therefore AB \parallel DC$$

$\Rightarrow$  In quad  $ABCD$  since  $AB \parallel DC \Rightarrow ABCD$  is a trapezium.

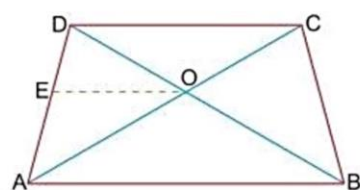


Fig. 7.13

6.  $E$  is a point on the side  $AD$  produced of a parallelogram  $ABCD$  and  $BE$  intersects  $CD$  at  $F$ . Show that  $\triangle ABE \sim \triangle CFB$ .

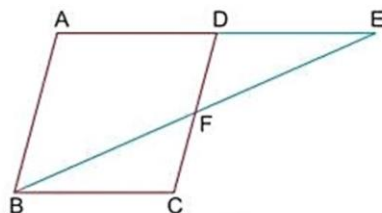


Fig. 7.14

Sol. In  $\triangle ABE$  and  $\triangle CFB$ , we have

$$\angle AEB = \angle CBF \quad \text{(Alternate angles)}$$

$$\angle A = \angle C \quad \text{(Opposite angles of a parallelogram)}$$

$$\therefore \triangle ABE \sim \triangle CFB \quad \text{(By AA criterion of similarity)}$$

7.  $CD$  and  $GH$  are respectively the bisectors of  $\angle ACB$  and  $\angle EGF$  such that  $D$  and  $H$  lie on sides  $AB$  and  $FE$  of  $\triangle ABC$  and  $\triangle EFG$ . If  $\triangle ABC \sim \triangle EFG$ , show that

(i)  $\frac{CD}{GH} = \frac{AC}{FG}$

(ii)  $\triangle DCB \sim \triangle HGE$

(iii)  $\triangle DCA \sim \triangle HGF$

Sol.  $\triangle ABC \sim \triangle EFG$ ,

$\Rightarrow \angle A = \angle F$

$\angle B = \angle E$

$\angle C = \angle G$

and  $\frac{AB}{FE} = \frac{BC}{EG} = \frac{AC}{FG}$

(i) In  $\triangle ACD$  and  $\triangle FGH$

$\angle A = \angle F$

and  $\angle 1 = \angle 2$

$\therefore \triangle ACD \sim \triangle FGH$

$\Rightarrow \frac{CD}{GH} = \frac{AC}{FG}$

(ii)  $\frac{CD}{GH} = \frac{AC}{FG}$

But  $\frac{AC}{FG} = \frac{BC}{EG}$

$\therefore \frac{CD}{GH} = \frac{BC}{EG}$

In  $\triangle DCB \sim \triangle HGE$

$\angle 3 = \angle 4$

and  $\frac{CD}{GH} = \frac{BC}{EG}$

$\therefore \triangle DCB \sim \triangle HGE$

(iii) In  $\triangle DCA$  and  $\triangle HGF$ ,

$\angle 1 = \angle 2$

and  $\frac{CD}{GH} = \frac{AC}{FG}$

$\Rightarrow \triangle DCA \sim \triangle HGF$

[Given]

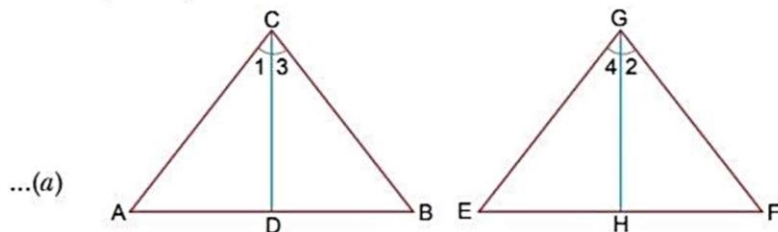


Fig. 7.15

[Given]

$[\frac{1}{2} \angle C = \frac{1}{2} \angle G]$

[AA Similarity]

[Corresponding sides of similar triangles]

[Proved above]

[From (a)]

$[\frac{1}{2} \angle C = \frac{1}{2} \angle G]$

[Proved above]

[SAS Similarity]

$[\frac{1}{2} \angle C = \frac{1}{2} \angle G]$

[Proved above]

[SAS Similarity]

8. In the given Fig. 7.16,  $AB = AC$ .  $E$  is a point on  $CB$  produced. If  $AD$  is perpendicular to  $BC$  and  $EF$  perpendicular to  $AC$ , prove that  $\triangle ABD$  is similar to  $\triangle ECF$ . [CBSE 2019 (30/5/1)]

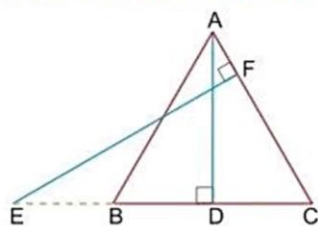


Fig. 7.16



<b>Sol.</b> $AB = AC \Rightarrow \angle C = \angle B$	... (1)	1
In $\triangle ABD$ & $\triangle ECF$ ,		
$\angle ADB = \angle EFC$ (each $90^\circ$ )		1
$\angle ABD = \angle ECF$ (by (1))		1
By AA similarity		
$\triangle ABD \sim \triangle ECF$		1

[CBSE Marking Scheme 2019]

9. A vertical pole of length 6 m casts a shadow 4 m long on the ground and at the same time a tower casts a shadow 28 m long. Find the height of the tower.

**Sol.** Let  $AB$  be a vertical pole of length 6 m and  $BC$  be its shadow and  $DE$  be tower and  $EF$  be its shadow. Join  $AC$  and  $DF$ .

Now, in  $\triangle ABC$  and  $\triangle DEF$ , we have

$$\angle B = \angle E = 90^\circ$$

$$\angle C = \angle F \quad (\text{Angle of elevation of the Sun})$$

$$\therefore \triangle ABC \sim \triangle DEF \quad (\text{By AA criterion of similarity})$$

Thus,  $\frac{AB}{DE} = \frac{BC}{EF}$

$$\Rightarrow \frac{6}{h} = \frac{4}{28} \quad (\text{Let } DE = h)$$

$$\Rightarrow \frac{6}{h} = \frac{1}{7} \quad \Rightarrow \quad h = 42$$

Hence, height of tower,  $DE = 42$  m

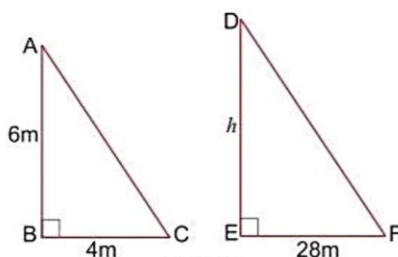


Fig. 7.17

10.  $ABCD$  is a trapezium in which  $AB \parallel DC$  and its diagonals intersect each other at the point  $O$ .

Show that  $\frac{AO}{BO} = \frac{CO}{DO}$ .

**Sol.** **Given:**  $ABCD$  is a trapezium, in which  $AB \parallel DC$  and its diagonals intersect each other at the point  $O$ .

**To prove:**  $\frac{AO}{BO} = \frac{CO}{DO}$

**Construction:** Through  $O$ , draw  $OE \parallel AB$  i.e.,  $OE \parallel DC$ .

**Proof:** In  $\triangle ADC$ , we have  $OE \parallel DC$  (Construction)

$\therefore$  By Basic Proportionality Theorem, we have

$$\frac{AE}{ED} = \frac{AO}{CO} \quad \dots(i)$$

Now, in  $\triangle ABD$ , we have  $OE \parallel AB$  (Construction)

$\therefore$  By Basic Proportionality Theorem, we have

$$\frac{ED}{AE} = \frac{DO}{BO} \quad \Rightarrow \quad \frac{AE}{ED} = \frac{BO}{DO} \quad \dots(ii)$$

From (i) and (ii), we have

$$\frac{AO}{CO} = \frac{BO}{DO} \quad \Rightarrow \quad \frac{AO}{BO} = \frac{CO}{DO}$$

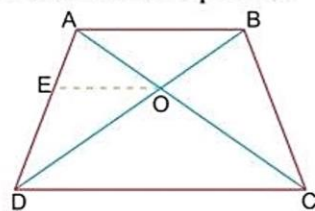


Fig. 7.18

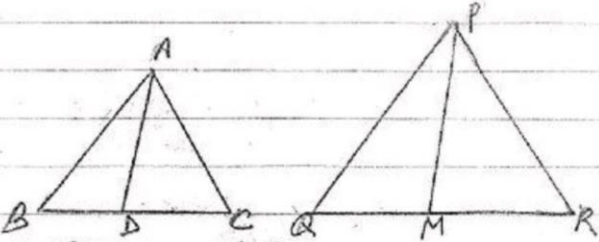
11.  $AD$  and  $PM$  are median of triangles  $\triangle ABC$  and  $\triangle PQR$  respectively where  $\triangle ABC \sim \triangle PQR$ .

Prove that  $\frac{AB}{PQ} = \frac{AD}{PM}$ .

[CBSE 2019(30/3/2)]

Sol.

17. Given,  
 $\triangle ABC \sim \triangle PQR$ .  
 $AD$  and  $PM$   
 are medians of  $\triangle ABC$  and  $\triangle PQR$  respectively.



Since,  $\triangle ABC \sim \triangle PQR$   
 $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$  — (1)

$D$  is the midpoint of  $BC$  ( $AD$  is median)  
 $M$  is the midpoint of  $QR$  ( $PM$  is median)

$\therefore BC = 2BD$   
 $QR = 2QM$  } (2)

$\therefore \frac{AB}{PQ} = \frac{BC}{QR}$  [from (1)]

$\Rightarrow \frac{AB}{PQ} = \frac{2BD}{2QM}$  [from (2)]

$\Rightarrow \frac{AB}{PQ} = \frac{BD}{QM} \Rightarrow \triangle ABD \sim \triangle PQM$  — (3)  
 That is,  $\frac{AB}{PQ} = \frac{BD}{QM} = \frac{AD}{PM}$

$\frac{AB}{PQ} = \frac{AD}{PM}$  hence proved!

[Topper's Answer 2019]

## Multiple Choice Questions

Choose and write the correct option in the following questions.

1.  $D$  and  $E$  are respectively the points on the sides  $AB$  and  $AC$  of a triangle  $ABC$  such that  $AD = 3$  cm,  $BD = 5$  cm,  $BC = 12.8$  cm and  $DE \parallel BC$ . Then length of  $DE$  (in cm) is
- (a) 4.8 cm (b) 7.6 cm  
 (c) 19.2 cm (d) 2.5 cm

2. Two similar figures are shown.

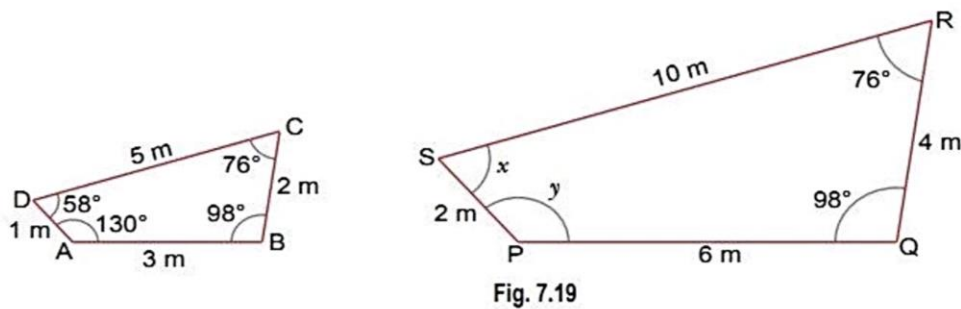


Fig. 7.19

What are the values of  $x$  and  $y$ ?

- (a)  $x = 58^\circ, y = 130^\circ$  (b)  $x = 98^\circ, y = 76^\circ$  (c)  $x = 82^\circ, y = 84^\circ$  (d)  $x = 130^\circ, y = 84^\circ$

3. Consider the figure below.

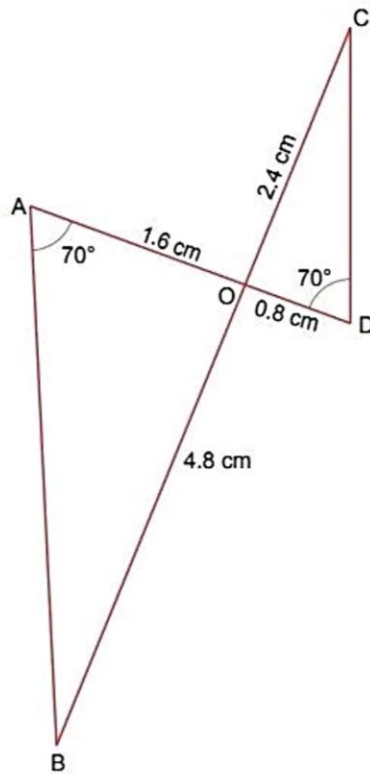


Fig. 7.20

Which of the following statement is correct about the triangles in the figure?

- (a)  $\triangle AOB \sim \triangle DOC$  because  $\frac{AO}{DO} = \frac{BO}{CO}$   
 (b)  $\triangle AOB \sim \triangle DOC$  because  $\angle AOB = \angle DOC$   
 (c)  $\triangle AOB \sim \triangle DOC$  because  $\frac{AO}{DO} = \frac{BO}{CO}$  and  $\angle BAO = \angle CDO$   
 (d)  $\triangle AOB \sim \triangle DOC$  because  $\frac{AO}{DO} = \frac{BO}{CO}$  and  $\angle AOB = \angle DOC$
4. In Fig. 7.21, two line segments  $AC$  and  $BD$  intersect each other at the point  $P$  such that  $PA = 6$  cm,  $PB = 3$  cm,  $PC = 2.5$  cm,  $PD = 5$  cm,  $\angle APB = 50^\circ$  and  $\angle CDP = 30^\circ$ . Then,  $\angle PBA$  is equal to  
 [NCERT Exemplar]

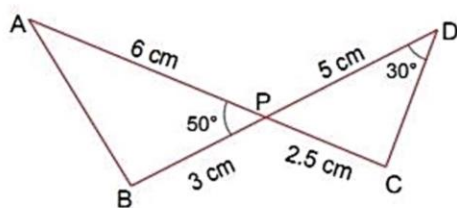


Fig. 7.21

- (a)  $50^\circ$                       (b)  $30^\circ$                       (c)  $60^\circ$                       (d)  $100^\circ$

5. In the given figure,  $QR \parallel AB$ ,  $RP \parallel BD$ ,  $CQ = x + 2$ ,  $QA = x$ ,  $CP = 5x + 4$ ,  $PD = 3x$ .

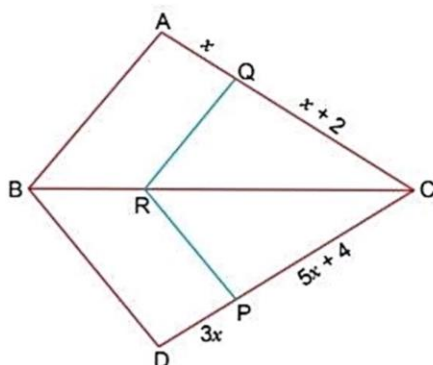


Fig. 7.22

The value of  $x$  is

- (a) 1                              (b) 6                              (c) 3                              (d) 9

6. In triangles  $ABC$  and  $DEF$ ,  $\angle B = \angle E$ ,  $\angle F = \angle C$  and  $AB = 3DE$ . Then, the two triangles are  
[NCERT Exemplar]

- (a) congruent but not similar                      (b) similar but not congruent  
(c) neither congruent nor similar                      (d) congruent as well as similar

7. It is given that  $\triangle ABC \sim \triangle DFE$ ,  $\angle A = 30^\circ$ ,  $\angle C = 50^\circ$ ,  $AB = 5$  cm,  $AC = 8$  cm and  $DF = 7.5$  cm. Then, the following is true:  
[NCERT Exemplar]

- (a)  $DE = 12$  cm,  $\angle F = 50^\circ$                       (b)  $DE = 12$  cm,  $\angle F = 100^\circ$   
(c)  $EF = 12$  cm,  $\angle D = 100^\circ$                       (d)  $EF = 12$  cm,  $\angle D = 30^\circ$

8. Rohit is 6 feet tall. At an instant, his shadow is 5 feet long. At the same instant, the shadow of a pole is 30 feet long. How tall is the pole?

- (a) 12 feet                      (b) 24 feet                      (c) 30 feet                      (d) 36 feet

9. In the following figure,  $Q$  is a point on  $PR$  and  $S$  is a point on  $TR$ .  $QS$  is drawn and  $\angle RPT = \angle RQS$ .  
[CBSE Question Bank]

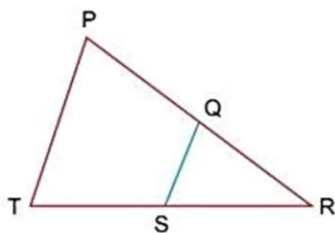


Fig. 7.23

Which of these criteria can be used to prove that  $\triangle RSQ$  is similar to  $\triangle RTP$ ?

- (a) AAA similarity criterion                      (b) SAS similarity criterion  
(c) SSS similarity criterion                      (d) None of these

10. Shown below are three triangles. The measures of two adjacent sides and included angle are given for each triangle. Which of these triangles are similar? [Competency Based Question]

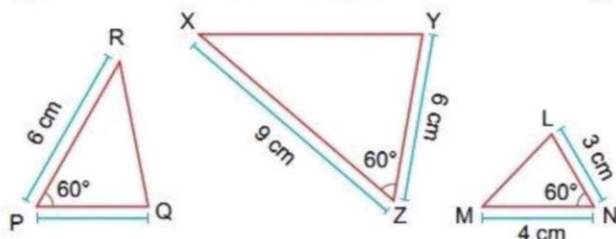


Fig. 7.24

- (a)  $\triangle RPQ$  and  $\triangle XZY$   
 (b)  $\triangle RPQ$  and  $\triangle MNL$   
 (c)  $\triangle XZY$  and  $\triangle MNL$   
 (d)  $\triangle RPQ$ ,  $\triangle XZY$  and  $\triangle MNL$  are similar to one another.
11. In the figure below,  $PQ \parallel CB$ .

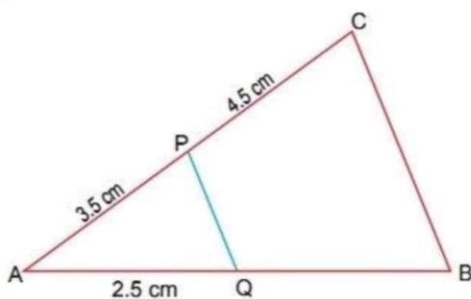


Fig. 7.25

To the nearest tenth, what is the length of  $QB$ ?

- (a) 1.4 cm  
 (b) 1.7 cm  
 (c) 3.2 cm  
 (d) 2.2 cm
12. In the figure given below,  $DE \parallel AC$  and  $DF \parallel AE$ . Which of these is equal to  $\frac{BF}{FE}$ ?

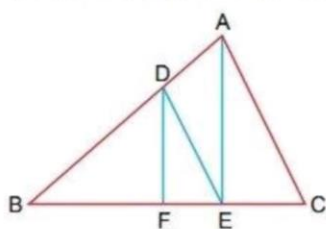


Fig. 7.26

- (a)  $\frac{DF}{AE}$   
 (b)  $\frac{BE}{EC}$   
 (c)  $\frac{BA}{AC}$   
 (d)  $\frac{FE}{EC}$

**Answers**

1. (a)      2. (a)      3. (d)      4. (d)      5. (a)      6. (b)      7. (b)  
 8. (d)      9. (a)      10. (a)      11. (c)      12. (b)

## Very Short Answer Questions

Each of the following questions are of 1 mark.

1. In  $\triangle ABC$ , if  $X$  and  $Y$  are points on  $AB$  and  $AC$  respectively such that  $\frac{AX}{XB} = \frac{3}{4}$ ,  $AY = 5$  and  $YC = 9$ , then state whether  $XY$  and  $BC$  are parallel or not.

Sol. It is given that

$$\frac{AX}{XB} = \frac{3}{4}, AY = 5 \text{ and } YC = 9$$

We have,  $\frac{AY}{YC} = \frac{5}{9}$

Since,  $\frac{AX}{XB} = \frac{3}{4} \neq \frac{5}{9} = \frac{AY}{YC}$

$$\Rightarrow \frac{AX}{XB} \neq \frac{AY}{YC}$$

Hence  $XY$  is not parallel to  $BC$ .

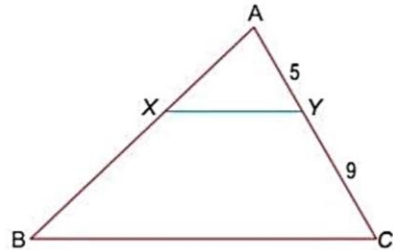


Fig. 7.27

2.  $A$  and  $B$  are respectively the points on the sides  $PQ$  and  $PR$  of a  $\triangle PQR$  such that  $PQ = 12.5$  cm,  $PA = 5$  cm,  $BR = 6$  cm, and  $PB = 4$  cm. Is  $AB \parallel QR$ ? Give reason.

Sol. Yes,  $\frac{PA}{AQ} = \frac{5}{12.5 - 5} = \frac{5}{7.5} = \frac{2}{3}$

$$\frac{PB}{BR} = \frac{4}{6} = \frac{2}{3}$$

Since  $\frac{PA}{AQ} = \frac{PB}{BR} = \frac{2}{3}$

$$\therefore AB \parallel QR$$

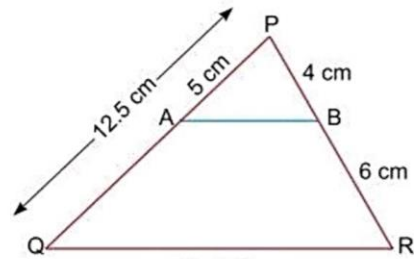


Fig. 7.28

3. In the figure, if  $\angle ACB = \angle CDA$ ,  $AC = 6$  cm and  $AD = 3$  cm, then find the length of  $AB$ . [CBSE Sample Paper 2020]

Sol.  $\triangle ACB \sim \triangle ADC$  (AA criterion)

$$\Rightarrow \frac{AC}{AD} = \frac{AB}{AC} \Rightarrow \frac{6}{3} = \frac{AB}{6} \Rightarrow AB = 6 \times 2$$

$$\therefore AB = 12 \text{ cm}$$

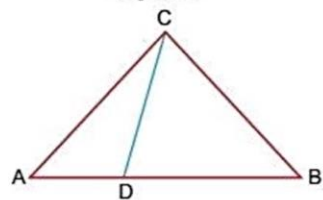


Fig. 7.29

4. Observe the right triangle  $ABC$ , right angled at  $B$  as shown below. What is the length of  $PC$ ?

Sol. We have

In  $\triangle APB$  and  $\triangle ABC$

$$\angle APB = \angle ABC = 90^\circ$$

$$\angle BAP = \angle BAC \quad (\text{Common})$$

$$\therefore \triangle APB \sim \triangle ABC \quad (\text{By AA similarity criteria})$$

$$\therefore \frac{AB}{AC} = \frac{AP}{AB} \Rightarrow AB^2 = AC \cdot AP$$

$$\Rightarrow 25 = (2x + 5) \cdot x$$

$$\Rightarrow 25 = 2x^2 + 5x \Rightarrow 2x^2 + 5x - 25 = 0$$

$$\Rightarrow 2x^2 + 10x - 5x - 25 = 0 \Rightarrow 2x(x + 5) - 5(x + 5) = 0$$

$$\Rightarrow (x + 5)(2x - 5) = 0$$

$$\Rightarrow 2x - 5 = 0 \quad (\because x + 5 \neq 0 \Rightarrow x \neq -5 \text{ length cannot be negative})$$

$$\therefore x = \frac{5}{2} = 2.5$$

$$\text{Length of } PC = x + 5 = 2.5 + 5 = 7.5 \text{ cm}$$

[Competency Based Question]

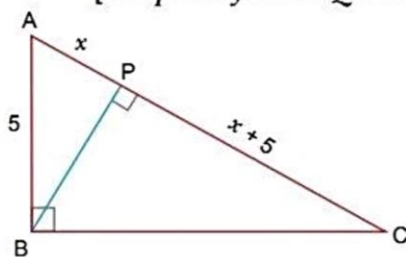


Fig. 7.30

### Short Answer Questions-I

Each of the following questions are of 2 marks.

1. In Fig. 7.31,  $DE \parallel AC$  and  $DC \parallel AP$ , Prove that  $\frac{BE}{EC} = \frac{BC}{CP}$ .

[CBSE 2020 (30/1/1)]

Sol. We have,

In  $\triangle ABC$ ,  $DE \parallel AC$

$$\therefore \frac{BD}{DA} = \frac{BE}{EC} \quad \dots(i)$$

Also, in  $\triangle ABP$ ,  $DC \parallel AP$

$$\therefore \frac{BD}{DA} = \frac{BC}{CP} \quad \dots(ii)$$

From (i) and (ii), we have

$$\frac{BE}{EC} = \frac{BC}{CP}$$

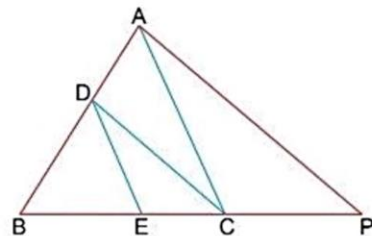


Fig. 7.31

2. In Fig. 7.32,  $DE \parallel BC$ . If  $AD = x$ ,  $DB = x - 2$ ,  $AE = x + 2$  and  $EC = x - 1$ , find the value of  $x$ .

Sol. In  $\triangle ABC$ , we have  $DE \parallel BC$

$$\therefore \frac{AD}{DB} = \frac{AE}{EC} \quad [\text{By Basic Proportionality Theorem}]$$

$$\Rightarrow \frac{x}{x-2} = \frac{x+2}{x-1} \Rightarrow x(x-1) = (x-2)(x+2)$$

$$\Rightarrow x^2 - x = x^2 - 4 \Rightarrow x = 4$$

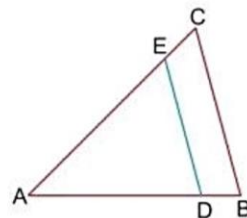


Fig. 7.32

3. The perimeters of two similar triangles are 30 cm and 20 cm respectively. If one side of the first triangle is 9 cm long, find the length of the corresponding side of the second triangle.

[CBSE 2020 (30/4/1)]

Sol. Let the side of other triangle be  $x$  cm.

$\therefore$  Ratio of perimeters of two similar triangles is equal to ratio of their corresponding sides.  $\frac{1}{2}$

$$\therefore \frac{9}{x} = \frac{30}{20} \quad 1$$

$$x = 6 \text{ cm} \quad \frac{1}{2}$$

[CBSE Marking Scheme 2020 (30/4/1)]

4. In Fig. 7.33,  $\triangle PQR$  is right-angled at  $P$ .  $M$  is a point on  $QR$  such that  $PM$  is perpendicular to  $QR$ . Show that  $PQ^2 = QM \times QR$ .

[CBSE 2020 (30/4/1)]

Sol. In  $\triangle RPQ$  and  $\triangle PMQ$ , we have

$$\angle RPQ = \angle PMQ = 90^\circ$$

$$\angle PQR = \angle MQP \quad (\text{Common angle})$$

$$\therefore \triangle RPQ \sim \triangle PMQ \quad (\text{By AA similarity criteria})$$

$$\therefore \frac{PQ}{QR} = \frac{QM}{PQ}$$

$$\Rightarrow PQ^2 = QM \times QR \quad \text{Proved}$$

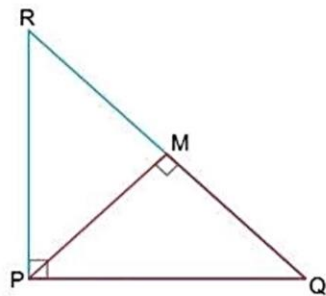


Fig. 7.33

5. In Fig. 7.34,  $ABC$  and  $DBC$  are two triangles on the same base  $BC$ . If  $AD$  intersects  $BC$  at  $O$ , show that

$$\frac{ar(\triangle ABC)}{ar(\triangle DBC)} = \frac{AO}{DO} \quad [CBSE 2020 (30/2/1)]$$

**Sol.** We have,  
 $\triangle ABC$  and  $\triangle DBC$  both lie on the same base  $BC$ .

To prove:  $\frac{ar(\triangle ABC)}{ar(\triangle DBC)} = \frac{AO}{DO}$

Construction: Draw  $AE \perp BC$  and  $DF \perp BC$

Proof: In  $\triangle AEO$  and  $\triangle DFO$ , we have  
 $\therefore \angle AOE = \angle DOF$  (Vertically opposite angles)  
 $\angle AEO = \angle DFO = 90^\circ$   
 $\therefore \triangle AEO \sim \triangle DFO$  (By AA similarity criterion)  
 $\therefore \frac{AE}{DF} = \frac{AO}{DO}$  ... (i)

Now,  $\frac{ar(\triangle ABC)}{ar(\triangle DBC)} = \frac{\frac{1}{2} \times BC \times AE}{\frac{1}{2} \times BC \times DF}$

$$\Rightarrow \frac{ar(\triangle ABC)}{ar(\triangle DBC)} = \frac{AE}{DF}$$

$$\Rightarrow \frac{ar(\triangle ABC)}{ar(\triangle DBC)} = \frac{AO}{DO}$$

(from (i)) Proved

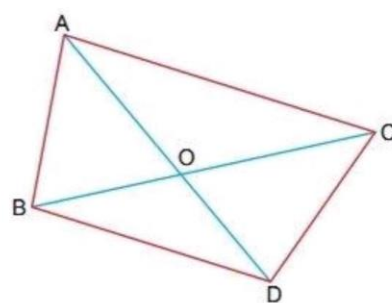


Fig. 7.34

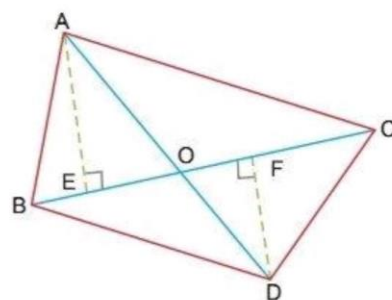


Fig. 7.35

### Short Answer Questions-II

Each of the following questions are of 3 marks.

1. In Fig. 7.36, if  $\triangle ABC \sim \triangle DEF$  and their sides of length (in cm) are marked along them, then find the lengths of sides of each triangle. [CBSE 2020 (30/2/1)]

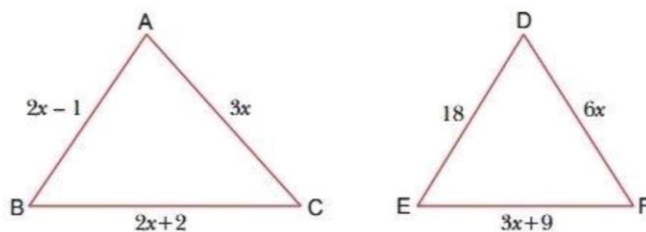


Fig. 7.36

**Sol.** Since,  $\triangle ABC \sim \triangle DEF$

$$\therefore \frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$$

$$\Rightarrow \frac{2x-1}{18} = \frac{2x+2}{3x+9} = \frac{3x}{6x}$$

$$\Rightarrow \frac{2x-1}{18} = \frac{2x+2}{3x+9} = \frac{1}{2}$$

Now, we have

$$\frac{2x-1}{18} = \frac{1}{2} \text{ and } \frac{2x+2}{3x+9} = \frac{1}{2}$$



$$\begin{array}{l|l} \Rightarrow 4x - 2 = 18 & \text{and, } 4x + 4 = 3x + 9 \\ \Rightarrow 4x = 20 & \Rightarrow x = \frac{20}{4} = 5 \\ \therefore x = 5 & \Rightarrow 4x - 3x = 9 - 4 = 5 \\ & \Rightarrow x = 5 \end{array}$$

$\therefore$  Length of sides of  $\triangle ABC$  are

$$AB = 2x - 1 = 2 \times 5 - 1 = 9 \text{ cm}$$

$$BC = 2x + 2 = 2 \times 5 + 2 = 12 \text{ cm}$$

and,  $AC = 3x = 3 \times 5 = 15 \text{ cm}$

$\therefore$  Length of sides of  $\triangle DEF$  are

$$DE = 18 \text{ cm, } EF = 3x + 9 = 3 \times 5 + 9 = 24 \text{ cm}$$

and  $DF = 6x = 6 \times 5 = 30 \text{ cm}$

2. In Fig. 7.37,  $\triangle FEC \cong \triangle GDB$  and  $\angle 1 = \angle 2$ . Prove that  $\triangle ADE \sim \triangle ABC$ .

[Competency Based Question]

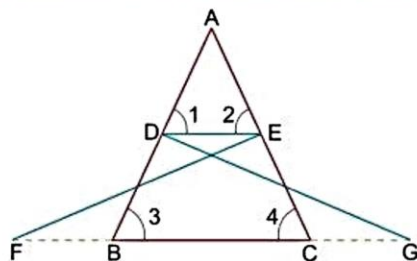


Fig. 7.37

Sol. Since,  $\triangle FEC \cong \triangle GDB$

$$\Rightarrow EC = BD \quad \dots(i)$$

It is given that

$$\angle 1 = \angle 2$$

$$\Rightarrow AE = AD \quad \left( \begin{array}{l} \text{Sides opposite to equal} \\ \text{angles are equal} \end{array} \right) \quad \dots(ii)$$

Dividing (ii) by (i), we have

$$\frac{AE}{EC} = \frac{AD}{BD}$$

$$\Rightarrow DE \parallel BC \quad (\text{By the converse of basic proportionality theorem})$$

$$\Rightarrow \angle 1 = \angle 3 \text{ and } \angle 2 = \angle 4 \quad (\text{Corresponding angles})$$

Thus, in  $\triangle$ 's  $ADE$  and  $ABC$ , we have

$$\angle A = \angle A \quad (\text{Common})$$

$$\angle 2 = \angle 4 \quad (\text{Proved above})$$

$$\Rightarrow \triangle ADE \sim \triangle ABC \quad (\text{By AA similarity})$$

3. In Fig. 7.38,  $\angle D = \angle E$  and  $\frac{AD}{DB} = \frac{AE}{EC}$ , prove that  $BAC$  is an isosceles triangle.

[CBSE 2020 (30/1/1)]

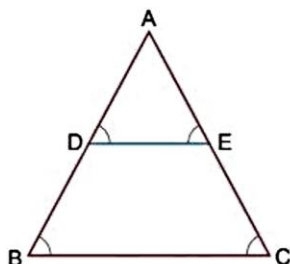


Fig. 7.38

**Sol.** Given,  $\angle D = \angle E$  and  $\frac{AD}{DB} = \frac{AE}{EC}$

$$\therefore \frac{AD}{DB} = \frac{AE}{EC} \Rightarrow DE \parallel BC$$

$\therefore \angle D = \angle B$  and  $\angle E = \angle C$  (Corresponding angles)

But it is given that  $\angle D = \angle E$

$$\angle B = \angle C \Rightarrow AC = AB \text{ (Sides opposite to equal angles are equal)}$$

$\therefore \triangle BAC$  is an isosceles triangle. Proved.

4. In Fig. 7.39,  $AB \parallel PQ \parallel CD$ ,  $AB = x$  units,  $CD = y$  units and  $PQ = z$  units. Prove that  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$ .

[Competency Based Question]

**Sol.** In  $\triangle ADB$  and  $\triangle PDQ$ ,

Since  $AB \parallel PQ$

$$\angle ABQ = \angle PQD \text{ (Corresponding angles)}$$

$$\angle ADB = \angle PDQ \text{ (Common)}$$

$$\triangle ADB \sim \triangle PDQ \text{ (By AA similarity)}$$

$$\therefore \frac{DQ}{DB} = \frac{PQ}{AB} \Rightarrow \frac{DQ}{DB} = \frac{z}{x}$$

Similarly,  $\triangle PBQ \sim \triangle CBD$

$$\text{and } \frac{BQ}{BD} = \frac{PQ}{CD} \Rightarrow \frac{BQ}{BD} = \frac{z}{y}$$

Adding (i) and (ii), we get

$$\frac{z}{x} + \frac{z}{y} = \frac{DQ + BQ}{DB} = \frac{BD}{BD}$$

$$\frac{z}{x} + \frac{z}{y} = 1 \Rightarrow \frac{1}{x} + \frac{1}{y} = \frac{1}{z}$$

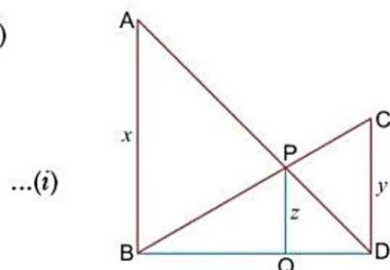


Fig. 7.39 ... (ii)

5. In Fig. 7.40,  $ABCD$  is a trapezium with  $AB \parallel DC$ . If  $\triangle AED$  is similar to  $\triangle BEC$ , prove that  $AD = BC$ .

**Sol.** In  $\triangle EDC$  and  $\triangle EBA$  we have

$$\angle 1 = \angle 2 \text{ (Alternate angles)}$$

$$\angle 3 = \angle 4 \text{ (Alternate angles)}$$

and  $\angle CED = \angle AEB$  (Vertically opposite angles)

$\therefore \triangle EDC \sim \triangle EBA$  (By AA criterion of similarity)

$$\Rightarrow \frac{ED}{EB} = \frac{EC}{EA} \Rightarrow \frac{ED}{EC} = \frac{EB}{EA} \dots (i)$$

It is given that  $\triangle AED \sim \triangle BEC$ .

$$\therefore \frac{ED}{EC} = \frac{EA}{EB} = \frac{AD}{BC} \dots (ii)$$

From (i) and (ii), we get

$$\frac{EB}{EA} = \frac{EA}{EB} \Rightarrow (EB)^2 = (EA)^2 \Rightarrow EB = EA$$

Substituting  $EB = EA$  in (ii), we get

$$\frac{EA}{EA} = \frac{AD}{BC} \Rightarrow \frac{AD}{BC} = 1 \Rightarrow AD = BC$$

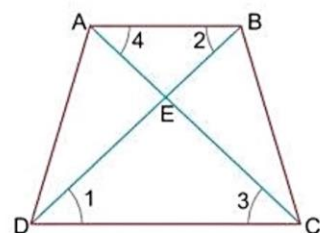


Fig. 7.40

## Long Answer Questions

Each of the following questions are of 5 marks.

1. Prove that, if a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio. [CBSE 2019 (30/2/1)]

**Sol. Given:** A triangle  $ABC$  in which a line parallel to side  $BC$  intersects other two sides  $AB$  and  $AC$  at  $D$  and  $E$  respectively.

**To Prove:**  $\frac{AD}{DB} = \frac{AE}{EC}$

**Construction:** Join  $BE$  and  $CD$  and then draw  $DM \perp AC$  and  $EN \perp AB$ .

**Proof:** Area of  $\triangle ADE = \left(\frac{1}{2} \text{ base} \times \text{height}\right)$

So,  $ar(\triangle ADE) = \frac{1}{2} (AD \times EN)$

and  $ar(\triangle BDE) = \frac{1}{2} (DB \times EN)$

Similarly,  $ar(\triangle ADE) = \frac{1}{2} (AE \times DM)$

and  $ar(\triangle DEC) = \frac{1}{2} (EC \times DM)$

Therefore,  $\frac{ar(\triangle ADE)}{ar(\triangle BDE)} = \frac{\frac{1}{2} AD \times EN}{\frac{1}{2} DB \times EN} = \frac{AD}{DB} \quad \dots(i)$

and  $\frac{ar(\triangle ADE)}{ar(\triangle DEC)} = \frac{\frac{1}{2} AE \times DM}{\frac{1}{2} EC \times DM} = \frac{AE}{EC} \quad \dots(ii)$

Now,  $\triangle BDE$  and  $\triangle DEC$  are on the same base  $DE$  and between the same parallel lines  $BC$  and  $DE$ .

So,  $ar(\triangle BDE) = ar(\triangle DEC) \quad \dots(iii)$

Therefore, from (i), (ii) and (iii) we have,  $\frac{AD}{DB} = \frac{AE}{EC}$ .

2. In Fig. 7.43,  $P$  is the mid-point of  $BC$  and  $Q$  is the mid-point of  $AP$ . If  $BQ$  when produced meets  $AC$  at  $R$ , prove that  $RA = \frac{1}{3} CA$ .

**Sol. Given:** In  $\triangle ABC$ ,  $P$  is the mid-point of  $BC$ ,  $Q$  is the mid-point of  $AP$  such that  $BQ$  produced meets  $AC$  at  $R$ .

**To prove:**  $RA = \frac{1}{3} CA$

**Construction:** Draw  $PS \parallel BR$ , meeting  $AC$  at  $S$ .

**Proof:** In  $\triangle BCR$ ,  $P$  is the mid-point of  $BC$  and  $PS \parallel BR$

$\therefore S$  is the mid-point of  $CR$ .

$\Rightarrow CS = SR \quad \dots(i)$

In  $\triangle APS$ ,  $Q$  is the mid-point of  $AP$  and  $QR \parallel PS$ .

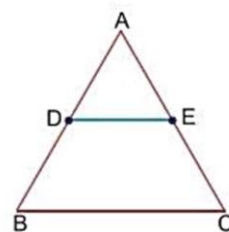


Fig. 7.41

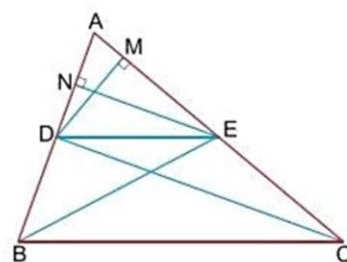


Fig. 7.42

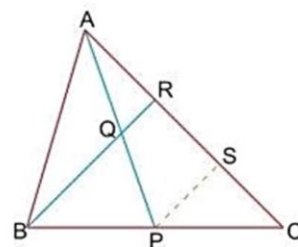


Fig. 7.43

$\therefore$   $R$  is the mid-point of  $AS$ .

$\Rightarrow AR = RS \quad \dots(ii)$

From (i) and (ii), we get

$AR = RS = SC$

$\Rightarrow AC = AR + RS + SC = 3AR \Rightarrow AR = \frac{1}{3}AC = \frac{1}{3}CA$

Hence proved.

3. Through the mid-point  $M$  of the side  $CD$  of a parallelogram  $ABCD$ , the line  $BM$  is drawn intersecting  $AC$  at  $L$  and  $AD$  produced to  $E$ . Prove that  $EL = 2BL$ .

Sol. In  $\triangle BMC$  and  $\triangle EMD$ , we have

$MC = MD \quad (\because M \text{ is the mid-point of } CD)$

$\angle CMB = \angle DME \quad (\text{Vertically opposite angles})$

and  $\angle MBC = \angle MED \quad (\text{Alternate angles})$

So, by *AAS* criterion of congruence, we have

$\triangle BMC \cong \triangle EMD$

$\Rightarrow BC = DE \quad (\text{CPCT})$

Also,  $BC = AD \quad (\because ABCD \text{ is a parallelogram})$

Now, in  $\triangle AEL$  and  $\triangle CBL$ , we have

$\angle ALE = \angle CLB \quad (\text{Vertically opposite angles})$

$\angle EAL = \angle BCL \quad (\text{Alternate angles})$

$\therefore \triangle AEL \sim \triangle CBL \quad (\text{By AA similarity})$

$\Rightarrow \frac{EL}{BL} = \frac{AE}{CB} \Rightarrow \frac{EL}{BL} = \frac{2BC}{BC} \quad (\because AE = AD + DE = BC + BC = 2BC)$

$\Rightarrow \frac{EL}{BL} = 2 \Rightarrow EL = 2BL$

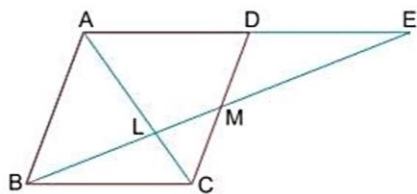


Fig. 7.44

### Case Study-based Questions

Each of the following questions are of 4 marks.

1. Read the following and answer any four questions from (i) to (v).

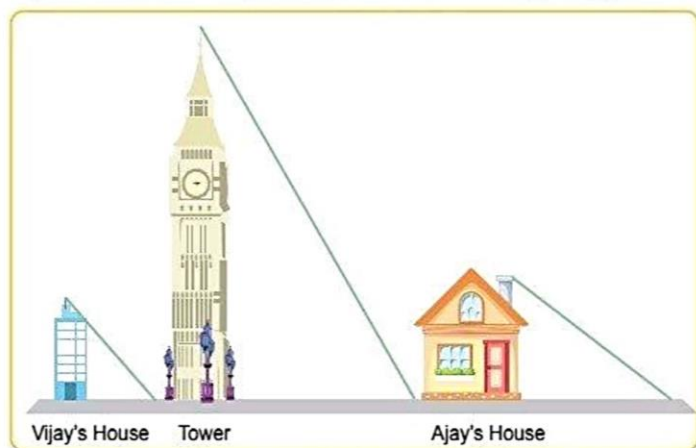


Fig. 7.45

Vijay is trying to find the average height of a tower near his house. He is using the properties of similar triangles. The height of Vijay's house is 20 m when Vijay's house casts a shadow 10 m long on the ground. At the same time, the tower casts a shadow 50 m long on the ground and the house of Ajay casts 20 m shadow on the ground.

[CBSE Question Bank]

- (i) What is the height of the tower?  
 (a) 20 m                      (b) 50 m                      (c) 100 m                      (d) 200 m
- (ii) What will be the length of the shadow of the tower when Vijay's house casts a shadow of 12m?  
 (a) 75 m                      (b) 50 m                      (c) 45 m                      (d) 60 m
- (iii) What is the height of Ajay's house?  
 (a) 30 m                      (b) 40 m                      (c) 50 m                      (d) 20 m
- (iv) When the tower casts a shadow of 40m, same time what will be the length of the shadow of Ajay's house?  
 (a) 16 m                      (b) 32 m                      (c) 20 m                      (d) 8 m
- (v) When the tower casts a shadow of 40m, same time what will be the length of the shadow of Vijay's house?  
 (a) 15 m                      (b) 32 m                      (c) 16 m                      (d) 8 m

**Sol.** (i) Let  $h$  m be the height of tower, therefore using property of similar triangle between two triangle *i.e.* for Vijay's house and for tower with shadows.

We have,

$$\frac{20}{h} = \frac{10}{50} \Rightarrow h = 100 \text{ m}$$

$\therefore$  Height of tower is 100 m.

$\therefore$  Option (c) is correct.

(ii) When Vijay's house casts a shadow of 12 m, we have

$$\frac{20}{h} = \frac{12}{x}, \text{ where } x \text{ is the length of shadow of tower.}$$

$$\Rightarrow \frac{20}{100} = \frac{12}{x} \Rightarrow x = 60 \text{ m}$$

$\therefore$  Option (d) is correct.

(iii) Let  $H$  m be the height of Ajay's house.

$$\therefore \frac{20}{10} = \frac{H}{20} \Rightarrow H = 40 \text{ m}$$

$\therefore$  Option (b) is correct.

(iv) When the tower casts a shadow of 40 m.

$$\therefore \frac{100}{40} = \frac{\text{Height of Ajay's house}}{\text{Length of shadow of Ajay's house}}$$

$$\Rightarrow \frac{5}{2} = \frac{40}{\text{Shadow length}}$$

$\Rightarrow$  Length of shadow of Ajay house = 16 m.

$\therefore$  Option (a) is correct.

(v) We have,

$$\frac{100}{40} = \frac{\text{Height of Vijay's house}}{\text{Length of its shadow}}$$

$$\Rightarrow \frac{5}{2} = \frac{20}{\text{Length of its shadow}}$$

$\Rightarrow$  Length of shadow of Vijay house = 8 m

$\therefore$  Option (d) is correct.

2. The legs of an iron table form two triangles as shown in the picture.

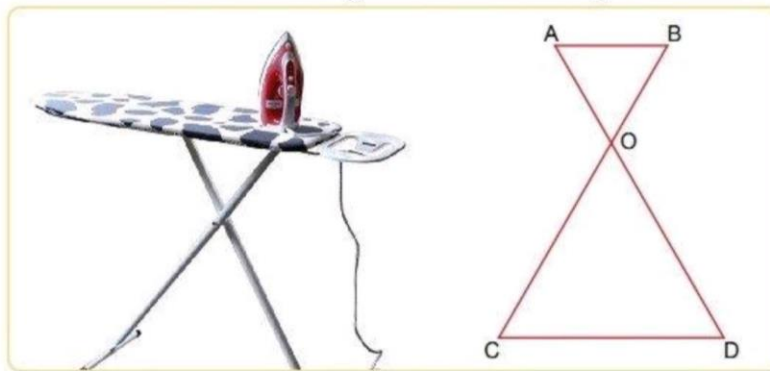


Fig. 7.46

Based on above information answer the following questions.

- (i) Which similarity criteria is applicable to prove the two triangles similar?  
 (ii) If  $AO = 30$  cm and  $OD = 45$  cm, then find perimeter ( $\triangle AOB$ ) : perimeter ( $\triangle COD$ ).  
 [Competency Based Question]

Sol. (i) Since  $AB \parallel CD$ ,  $\angle A = \angle D$  and  $\angle B = \angle C$  (Alternate interior angles)

Also,  $\angle AOB = \angle COD$  (Vertically opposite angles)

So,  $\triangle AOB \sim \triangle DOC$  (By AAA similarity criteria)

Hence AAA similarity criteria is applicable.

(ii)  $\frac{AO}{OD} = \frac{30}{45} = \frac{2}{3}$

Since  $\triangle AOB \sim \triangle DOC$

$$\Rightarrow \frac{\text{Perimeter } (\triangle AOB)}{\text{Perimeter } (\triangle DOC)} = \frac{AO}{OD} = \frac{2}{3} \quad (\because \text{Ratio of perimeters of two similar triangles is equal to ratio of their corresponding sides})$$

Hence, the ratio is 2 : 3.

## PROFICIENCY EXERCISE

### Objective Type Questions:

[1 mark each]

1. Choose and write the correct option in each of the following questions.

- (i) In Fig. 7.47 below,  $PQ \parallel CB$ .

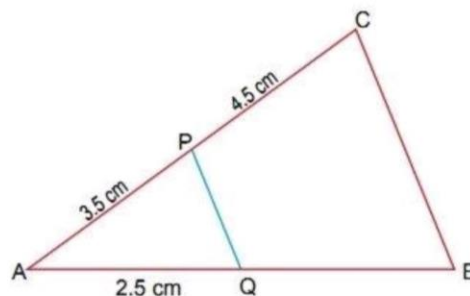


Fig. 7.47

To the nearest tenth, what is the length of  $QB$ ?

- (a) 1.4 cm      (b) 1.7 cm      (c) 1.8 cm      (d) 2.2 cm

(ii) Consider the Fig. 7.48 below.

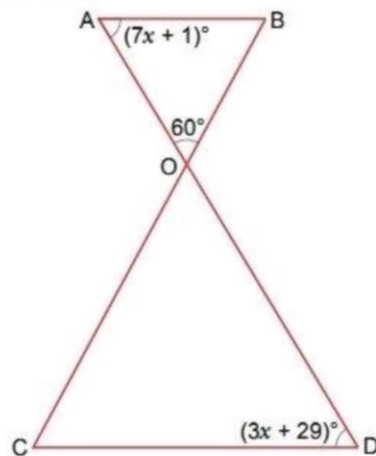


Fig. 7.48

Which of the following statement helps proving that triangle  $AOB$  is similar to triangle  $DOC$ ? [Competency Based Question]

- (i)  $\angle B = 70^\circ$ , and (ii)  $\angle C = 70^\circ$
- (a) Statement (i) alone is sufficient, but statement (ii) alone is not sufficient.  
 (b) Statement (ii) alone is sufficient, but statement (i) alone is not sufficient.  
 (c) Either (i) or (ii) statement alone is sufficient.  
 (d) Both statements together is sufficient, but neither statement alone is sufficient.
- (iii) If  $\triangle ABC \sim \triangle EDF$  and  $\triangle ABC$  is not similar to  $\triangle DEF$ , then which of the following is not true? [NCERT Exemplar]
- (a)  $BC \cdot EF = AC \cdot FD$  (b)  $AB \cdot EF = AC \cdot DE$   
 (c)  $BC \cdot DE = AB \cdot EF$  (d)  $BC \cdot DE = AB \cdot FD$
- (iv) Ankit is 5 feet tall. He places a mirror on the ground and moves until he can see the top of a building. At the instant when Ankit is 2 feet from the mirror, the building is 48 feet from the mirror. How tall is the building?
- (a) 96 feet (b) 120 feet  
 (c) 180 feet (d) 240 feet

■ **Very Short Answer Questions:**

[1 mark each]

2. In Fig. 7.49,  $GC \parallel BD$  and  $GE \parallel BF$ . If  $AC = 3$  cm and  $CD = 7$  cm, then find the value of  $\frac{AE}{AF}$ . [CBSE 2019(C) (30/1/1)]

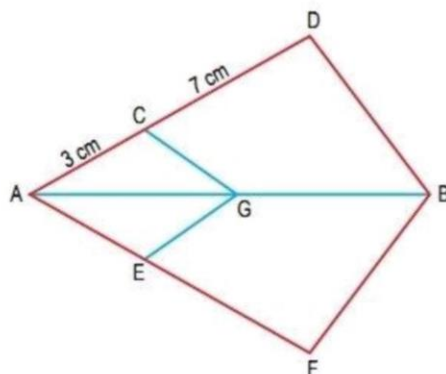


Fig. 7.49

3. In Fig. 7.50,  $DE \parallel BC$ . Find the length of side  $AD$ , given that  $AE = 1.8$  cm,  $BD = 7.2$  cm and  $CE = 5.4$  cm. [CBSE 2019 (30/2/1)]

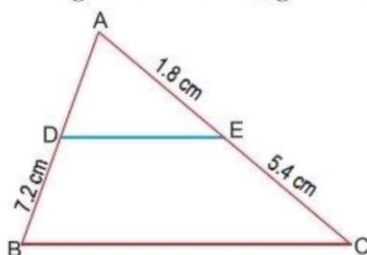


Fig. 7.50

4.  $A$  and  $B$  are respectively the points on the sides  $PQ$  and  $PR$  of a triangle  $PQR$  such that  $PQ = 10.5$  cm,  $PA = 4.5$  cm,  $BR = 8$  cm and  $PB = 6$  cm. Is  $AB \parallel QR$ ?
5. If in two right triangles, one of the acute angle of one triangle is equal to an acute angle of the other triangle, can you say that the two triangles will be similar?
6. It is given that  $\triangle DEF \sim \triangle RPQ$ . Is it true to say that  $\angle D = \angle R$  and  $\angle F = \angle P$ ? [NCERT Exemplar]

■ Short Answer Questions-I:

[2 marks each]

7.  $X$  is a point on the side  $BC$  of  $\triangle ABC$ .  $XM$  and  $XN$  are drawn parallel to  $AB$  and  $AC$  respectively meeting  $AB$  in  $N$  and  $AC$  in  $M$ .  $MN$  produced meets  $CB$  produced at  $T$ . Prove that  $TX^2 = TB \times TC$ . [CBSE 2018 (C) (30/1)]

8. In Fig. 7.51,  $\frac{OA}{OC} = \frac{OD}{OB}$ . Prove that  $\angle A = \angle C$  and  $\angle B = \angle D$ .

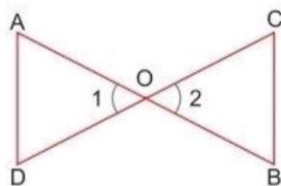


Fig. 7.51

9. Two poles of height 9 m and 15 m stand vertically upright on a plane ground. If the distance between their tops is 10m, then find the distance between their feet.
10.  $\triangle ABC \sim \triangle DEF$ . If  $AB = 4$  cm,  $BC = 3.5$  cm,  $CA = 2.5$  cm and  $DF = 7.5$  cm, then find perimeter of  $\triangle DEF$ .
11.  $AD$  is the bisector of  $\angle BAC$  in  $\triangle ABC$ . If  $AB = 10$  cm,  $AC = 6$  cm and  $BC = 12$  cm, then find  $BD$ .

■ Short Answer Questions-II:

[3 marks each]

12.  $ABCD$  is a trapezium with  $AB \parallel DC$ .  $E$  and  $F$  are points on non-parallel sides  $AD$  and  $BC$  respectively, such that  $EF \parallel AB$ . Show that  $\frac{AE}{ED} = \frac{BF}{FC}$ . [CBSE 2019 (C)(30/1/1)]
13. In  $\triangle ABC$ ,  $DE \parallel BC$ . If  $AD = 4x - 3$ ,  $AE = 8x - 7$ ,  $BD = 3x - 1$  and  $CE = 5x - 3$ , find the value of  $x$ .
14. In Fig. 7.52,  $P$  is the mid-point of  $EF$  and  $Q$  is the mid-point of  $DP$ . If  $EQ$  when produced meets  $DF$  at  $R$ , prove that  $RD = \frac{1}{3}DF$ . [Competency Based Question]

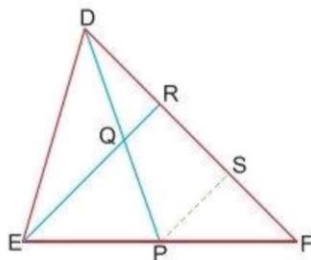


Fig. 7.52





**Answers**

1. (i) (c)      (ii) (c)      (iii) (c)      (iv) (b)  
 2. 3 : 10      3.  $AD = 2.4$  cm      4. Yes      5. Yes, by AA similarity  
 6. No      9. 8 m      10. 30 cm      11.  $BD = 7.5$  cm      13.  $x = 1$  or  $x = \frac{1}{2}$   
 15. 9 m      17. 11 or 8

**Self-Assessment**

Time allowed: 1 hour

Max. marks: 40

**SECTION A**

1. Choose and write the correct option in the following questions.

(3 × 1 = 3)

(i) Observe the two triangles shown below.

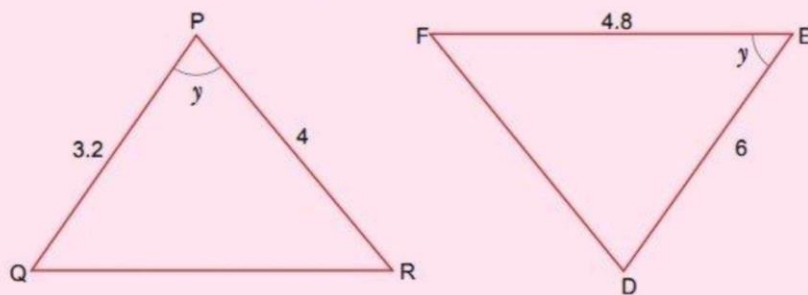


Fig. 7.58

Which statement is correct?

- (a) Triangles are similar by SSA.  
 (b) Triangles are similar by SAS.  
 (c) Triangles are not similar as sides are not in proportion.  
 (d) No valid conclusion about similarity of triangles can be made as angle measures are not given.
- (ii) The straight line distance between A and B is (Fig. 7.59)

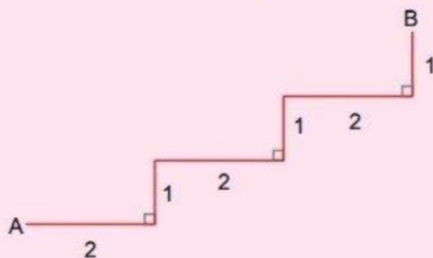


Fig. 7.59

[Competency Based Question]

- (a)  $5\sqrt{3}$  units      (b) 5 units      (c)  $3\sqrt{5}$  units      (d)  $5\sqrt{2}$  units
- (iii) If S is a point on side PQ of a  $\Delta PQR$  such that  $PS = QS = RS$ , then [NCERT Exemplar]  
 (a)  $PR \cdot QR = RS^2$       (b)  $QS^2 + RS^2 = QR^2$   
 (c)  $PR^2 + QR^2 = PQ^2$       (d)  $PS^2 + RS^2 = PR^2$

2. Solve the following questions. (2 × 1 = 2)

- (i) In triangle  $ABC$ ,  $D, E, F$  are the points on  $AB, AC, BC$  respectively such that  $AD = 3$  cm,  $AE = 5$  cm,  $BD = 4$  cm,  $CE = 4$  cm,  $CF = 2$  cm and  $BF = 2.5$  cm. Show that  $EF \parallel AB$ .
- (ii) If  $DE$  has been drawn parallel to side  $BC$  of  $\triangle ABC$  cutting  $AB$  and  $AC$  at points  $D$  and  $E$  respectively, such that  $\frac{AD}{DB} = \frac{3}{4}$ , then find the value of  $\frac{AE}{EC}$ .

**SECTION B**

■ Solve the following questions. (4 × 2 = 8)

3. If  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively of  $\triangle ABC$  and  $AB = 12$  cm,  $AD = 8$  cm,  $AE = 12$  cm,  $AC = 18$  cm then prove that  $DE \parallel BC$ .
4. The perimeters of two similar triangles  $ABC$  and  $PQR$  are 60 cm and 36 cm respectively. If  $PQ = 9$  cm, then find the length of  $AB$ .
5. In the Fig. 7.60,  $AD$  is the bisector of  $\angle BAC$ . If  $BC = 10$  cm,  $BD = 6$  cm,  $AC = 6$  cm, then find  $AB$ .

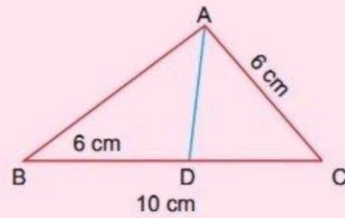


Fig. 7.60

6. In the given figure, find  $\angle P$ .

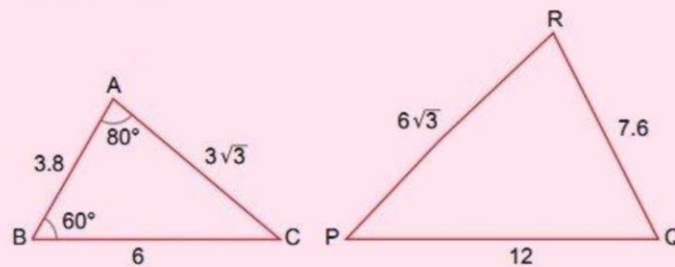


Fig. 7.61

■ Solve the following questions. (4 × 3 = 12)

7. Ankit of height 160 cm is going away from the lamp post at a speed of 2 m/sec. If the lamp post is 3.2 m above the ground find the length of his shadow after 5 seconds.
8. In the given figure  $\angle 1 = \angle 2$  and  $\angle 3 = \angle 4$ . Show that  $PT \cdot QR = PS \cdot ST$ .

[Competency Based Question]

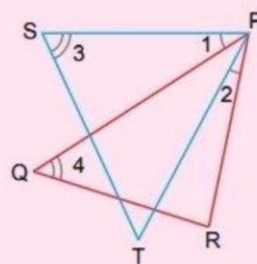


Fig. 7.62

9. In the given figure  $BC = 5$  cm,  $AC = 5.5$  cm and  $AB = 4.6$  cm.  $P$  and  $Q$  are points on  $AB$  and  $AC$  respectively such that  $PQ \parallel BC$ . If  $PQ = 2.5$  cm, find other sides of  $\Delta APQ$ .

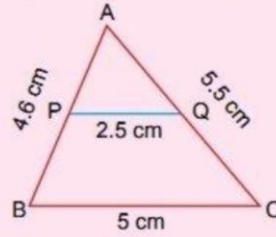


Fig. 7.63

10. In the given figure,  $\frac{AO}{OC} = \frac{BO}{OD} = \frac{1}{2}$  and  $AB = 5$  cm. Find the value of  $DC$ .

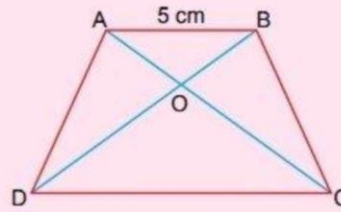


Fig. 7.64

■ Solve the following questions.

(3 × 5 = 15)

11.  $ABCD$  is quadrilateral in which,  $\frac{AB}{AD} = \frac{5}{3}$ .  $AM$  is the bisector of  $\angle BAD$  meeting  $BD$  at  $M$  and  $MN \parallel BC$ , then find (i)  $\frac{BM}{MD}$  (ii)  $\frac{DN}{NC}$ .

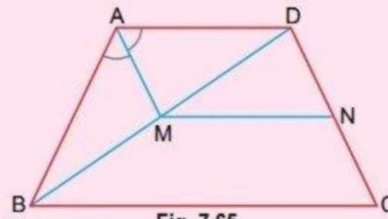


Fig. 7.65

12. In the given figure, if  $\Delta ABE \cong \Delta ACD$ , show that  $\Delta ADE \sim \Delta ABC$ .

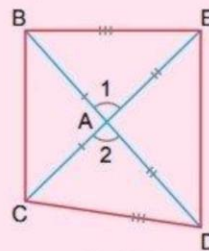


Fig. 7.66

13. In  $\Delta PQR$  and  $\Delta MST$ ,  $\angle P = 55^\circ$ ,  $\angle Q = 25^\circ$ ,  $\angle M = 100^\circ$  and  $\angle S = 25^\circ$ . Is  $\Delta QPR \sim \Delta TSM$ ? Why?

**Answers**

1. (i) (b)      (ii) (c)      (iii) (c)      2. (ii)  $\frac{3}{4}$       4. 15 cm  
 5.  $AB = 9$  cm      6.  $40^\circ$       7. 10 m      9.  $AP = 2.3$  cm and  $AQ = 2.75$  cm  
 10.  $DC = 10$  cm      11. (i)  $\frac{5}{3}$  (ii)  $\frac{3}{5}$       13. No, because of incorrect correspondence.

